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Supplemental Material

A High-Throughput Analysis of Ovarian Cycle Disruption by Mixtures of Aromatase Inhibitors

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References

Figure S1: Computational workflow.

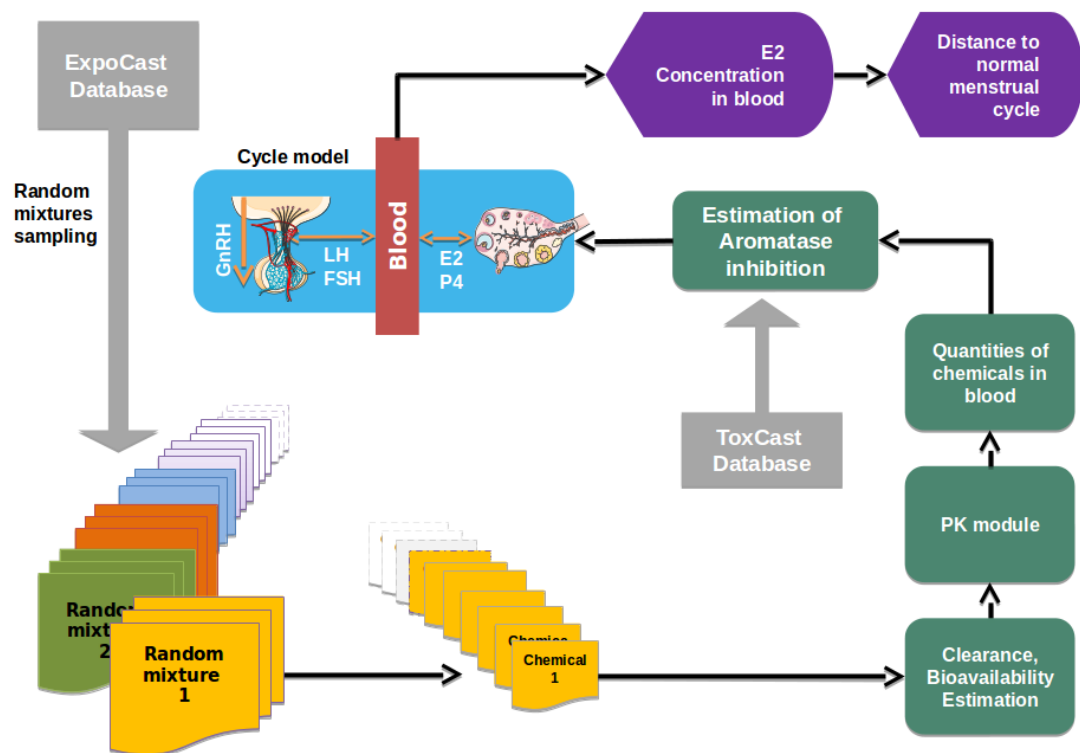


Figure S1. Computational workflow. Each box represents a task to be executed or a result obtained and arrows represent either data flow or execution dependencies between different tasks. Random mixtures of chemicals are sampled from ExpoCast. The kinetics of each chemical in the human body are computed using a one-compartment PK model. The resulting aromatase inhibition is computed from ToxCast dose-response information. The impact of that inhibition on the menstrual cycle is estimated using an ovarian cycle model adapted from Chen and Ward (2013).

Methods S1: PK modules of ACD/Labs.

The ACD/Oral Bioavailability module uses a combination of probabilistic and mechanistic models to predict oral bioavailability based on a dataset of oral bioavailability data for 788 substances. The module predicts the fraction of the specified dose that reaches systemic circulation after oral administration (F), with the possibility to explore dose-dependence of F . The default oral dose used in calculations is 50 mg. The mathematical model used for simulations in the Oral Bioavailability (and PK Explorer) modules is based on differential equations that consider solubility in the gastrointestinal tract, passive-absorption in jejunum, elimination (total body clearance), and volume of distribution. Simulations performed with the Oral Bioavailability module ignore first-pass metabolism in liver and gut. Quantitative F values are calculated as a ratio of AUCs after oral and intravenous administration. A number of endpoints affecting oral bioavailability are also predicted, including solubility (dose/solubility ratio), stability in acidic media, intestinal membrane permeability by passive or active transport (with a summary of transporters where relevant), P-gp efflux (multi-drug transporter P-glycoprotein) and first pass metabolism in the liver. For the majority of these parameters, ACD/Labs Percepta allows the user to assess the confidence in the predicted result by means of reliability index and/or displaying similar structures from the training set along with their experimental test results. Since the bioavailability predictions are based on a mechanistic simulation model rather than statistical fitting to data, the validation procedure was not based on a conventional training/test set approach. Instead, a set of clinical fraction absorbed (f_a) data together with dosage information for 28 drugs reported by Parrot and Lavé (2002) was used for validation purposes. The model performance was assessed qualitatively, by evaluating the accuracy of three-class classification (i.e., “low” for $f_a \leq 33\%$, “moderate” for $33\% < f_a < 66\%$, “high” for $f_a \geq 66\%$), and quantitatively, using the Residual Mean Square Error statistic and visual inspection of the correlation between observed and predicted f_a values for the drugs considered. For the majority of drugs, calculated values were in good agreement with clinical data, resulting in 80% correct classification and an RMSE equal to 17%.

ACD/PK Explorer is a tool for exploring pharmacokinetic relationships (e.g., F –Dose relationship) using physico-chemical parameters as inputs for calculations. Total body clearance rate constant (Ke) is among the required parameters of our PK model. Ke was estimated using a set of fragmental ionization class specific models. Hydrophobicity (logP) and ionization (pKa) are the principal descriptors for the prediction of Ke . These descriptors were calculated *in silico*. Technical details on those models and equations are not available since they are proprietary information of ACD/Labs.

Figure S1: Predictions of bioavailability (F) and total body clearance rate constant (K_e). The ACD/Labs Percepta Oral Bioavailability module was used for predictions of oral F values. F predictions depend on oral dose and are given for an array of doses. The module ACD/ PK Explorer was used for the prediction of K_e values.

ID	CAS	F (0.001 mg)	F (0.01 mg)	F (0.1 mg)	F (1 mg)	F (5 mg)	F (10 mg)	F (50 mg)	F (100 mg)	F (500 mg)	F (1000 mg)	K_e (min ⁻¹)
1	101-20-2	0.2805	0.2804	0.2798	0.2739	0.2505	0.2269	0.1342	0.0919	0.0295	0.0168	0.00083
2	101-80-4	0.9760	0.9760	0.9760	0.9759	0.9754	0.9748	0.9661	0.9486	0.5863	0.3625	0.002
3	112281-77-3	0.9907	0.9907	0.9907	0.9907	0.9903	0.9899	0.9826	0.9575	0.5201	0.3202	0.0011
4	112809-51-5	0.9919	0.9919	0.9919	0.9919	0.9917	0.9915	0.9880	0.9771	0.6065	0.3808	0.00041
5	114369-43-6	0.7271	0.7270	0.7261	0.7175	0.6807	0.6385	0.4214	0.2983	0.0986	0.0566	0.0011
6	115-39-9	0.2164	0.2164	0.2158	0.2104	0.1897	0.1694	0.0956	0.0644	0.0201	0.0114	0.00087
7	116255-48-2	0.9884	0.9884	0.9884	0.9882	0.9872	0.9856	0.9580	0.8774	0.3949	0.2374	0.0011
8	117-39-5	0.9533	0.9533	0.9533	0.9532	0.9528	0.9521	0.9429	0.9247	0.5982	0.3723	0.0062
9	1192-52-5	0.9942	0.9942	0.9942	0.9942	0.9942	0.9942	0.9942	0.9942	0.9938	0.9933	0.0015
10	120511-73-1	0.9916	0.9916	0.9916	0.9916	0.9915	0.9915	0.9910	0.9901	0.9455	0.7218	0.0009
11	125-84-8	0.9936	0.9936	0.9936	0.9936	0.9936	0.9936	0.9935	0.9932	0.9899	0.9812	0.0019
12	126-72-7	0.9908	0.9908	0.9908	0.9907	0.9904	0.9899	0.9826	0.9586	0.5198	0.3193	0.0012
13	126-86-3	0.9938	0.9938	0.9938	0.9938	0.9937	0.9935	0.9915	0.9862	0.6964	0.4480	0.0017
14	1260-17-9	0.0078	0.0078	0.0078	0.0078	0.0078	0.0078	0.0078	0.0078	0.0078	0.0078	0.0049
15	129-17-9	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0071
16	129453-61-8	0.0067	0.0067	0.0066	0.0064	0.0056	0.0049	0.0026	0.0017	0.0005	0.0003	0.0002
17	131341-86-1	0.9393	0.9393	0.9390	0.9360	0.9223	0.9039	0.7408	0.5798	0.2155	0.1264	0.0002
18	13171-00-1	0.9836	0.9836	0.9835	0.9830	0.9802	0.9759	0.9089	0.7791	0.3177	0.1886	0.0012
19	131860-33-8	0.9603	0.9603	0.9601	0.9581	0.9481	0.9337	0.7802	0.6097	0.2225	0.1298	0.00068

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20	13292-46-1	0.1755	0.1755	0.1755	0.1755	0.1755	0.1755	0.1755	0.1755	0.1754	0.1713	0.0019
21	133-06-2	0.8723	0.8723	0.8717	0.8665	0.8427	0.8128	0.6083	0.4543	0.1600	0.0930	0.0017
22	133-07-3	0.5715	0.5714	0.5705	0.5623	0.5282	0.4910	0.3167	0.2236	0.0742	0.0427	0.0015
23	133855-98-8	0.9064	0.9064	0.9059	0.9016	0.8814	0.8551	0.6557	0.4932	0.1743	0.1012	0.00075
24	137-26-8	0.9764	0.9764	0.9763	0.9750	0.9690	0.9603	0.8526	0.7011	0.2741	0.1619	0.0022
25	137-30-4	0.8689	0.8689	0.8689	0.8689	0.8689	0.8689	0.8689	0.8689	0.8689	0.8689	0.0032
26	14233-37-5	0.8501	0.8500	0.8494	0.8430	0.8143	0.7789	0.5556	0.4044	0.1376	0.0794	0.0014
27	15299-99-7	0.9827	0.9827	0.9826	0.9819	0.9785	0.9734	0.8969	0.7597	0.3053	0.1809	0.0014
28	155990-20-8	0.9920	0.9920	0.9920	0.9920	0.9920	0.9920	0.9920	0.9920	0.9919	0.9915	0.0013
29	15972-60-8	0.9952	0.9952	0.9952	0.9952	0.9952	0.9952	0.9950	0.9948	0.9901	0.9624	0.0019
30	16423-68-0	0.0002	0.0002	0.0002	0.0001	0.0001	0.0001	0.0001	0.0000	0.0000	0.0000	0.00065
31	175013-18-0	0.9892	0.9892	0.9892	0.9890	0.9882	0.9870	0.9656	0.8972	0.4116	0.2477	0.0012
32	17924-92-4	0.9958	0.9958	0.9958	0.9958	0.9958	0.9958	0.9953	0.9943	0.9495	0.7248	0.0022
33	1918-02-1	66.39	66.39	66.39	66.39	66.39	66.39	66.39	66.39	66.39	66.39	0.0025
34	199171-88-5	0.9916	0.9916	0.9916	0.9916	0.9916	0.9916	0.9913	0.9909	0.9811	0.9148	0.00099
35	2310-17-0	0.7593	0.7592	0.7584	0.7503	0.7153	0.6745	0.4547	0.3245	0.1083	0.0623	0.0014
36	2312-35-8	0.8301	0.8301	0.8294	0.8223	0.7913	0.7535	0.5266	0.3800	0.1280	0.0737	0.0013
37	2353-45-9	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0047
38	24169-02-6	0.6276	0.6275	0.6266	0.6173	0.5789	0.5366	0.3397	0.2372	0.0773	0.0442	0.00089
39	2425-06-1	0.5641	0.5641	0.5632	0.5544	0.5186	0.4797	0.3031	0.2121	0.0695	0.0398	0.0016
40	29091-21-2	0.2182	0.2182	0.2177	0.2127	0.1932	0.1739	0.1007	0.0685	0.0218	0.0124	0.00054
41	30399-84-9	0.9043	0.9042	0.9037	0.8990	0.8772	0.8488	0.6383	0.4740	0.1645	0.0952	0.0011

ID	CAS	F (0.001 mg)	F (0.01 mg)	F (0.1 mg)	F (1 mg)	F (5 mg)	F (10 mg)	F (50 mg)	F (100 mg)	F (500 mg)	F (1000 mg)	K_e (min ⁻¹)
42	311-45-5	0.9965	0.9965	0.9965	0.9965	0.9965	0.9965	0.9965	0.9964	0.9957	0.9940	0.0023
43	35554-44-0	0.9924	0.9924	0.9924	0.9924	0.9924	0.9923	0.9916	0.9903	0.8887	0.6276	0.0012
44	3844-45-9	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.007
45	43121-43-3	0.9919	0.9919	0.9919	0.9918	0.9917	0.9915	0.9889	0.9819	0.6581	0.4188	0.0012
46	49562-28-9	0.9326	0.9326	0.9322	0.9286	0.9116	0.8886	0.6955	0.5259	0.1858	0.1079	0.0016
47	50-41-9	0.9197	0.9197	0.9193	0.9151	0.8954	0.8692	0.6612	0.4919	0.1704	0.0986	0.00014
48	50594-66-6	0.6879	0.6878	0.6868	0.6771	0.6361	0.5904	0.3727	0.2590	0.0836	0.0477	0.00064
49	51630-58-1	0.0101	0.0101	0.0100	0.0098	0.0087	0.0077	0.0042	0.0028	0.0009	0.0005	0.0014
50	52-01-7	0.9256	0.9255	0.9251	0.9209	0.9011	0.8746	0.6651	0.4948	0.1714	0.0991	0.0027
51	520-18-3	0.9892	0.9892	0.9892	0.9892	0.9890	0.9888	0.9865	0.9819	0.8086	0.5408	0.0015
52	521-18-6	0.9647	0.9647	0.9645	0.9624	0.9521	0.9375	0.7852	0.6166	0.2272	0.1328	0.0036
53	53-16-7	0.9600	0.9600	0.9598	0.9578	0.9480	0.9342	0.7886	0.6236	0.2321	0.1360	0.0012
54	55219-65-3	0.9917	0.9917	0.9917	0.9917	0.9914	0.9910	0.9858	0.9684	0.5578	0.3462	0.0013
55	57-63-6	0.8500	0.8500	0.8493	0.8430	0.8149	0.7801	0.5593	0.4083	0.1395	0.0806	0.0011
56	577-11-7	0.8287	0.8286	0.8278	0.8198	0.7841	0.7411	0.4968	0.3509	0.1149	0.0658	0.0055
57	58-14-0	0.9688	0.9687	0.9686	0.9672	0.9600	0.9488	0.7915	0.6000	0.2057	0.1184	0.0014
58	58-89-9	0.9227	0.9227	0.9223	0.9188	0.9024	0.8808	0.7044	0.5441	0.1994	0.1167	0.0018
59	60168-88-9	0.8674	0.8673	0.8667	0.8610	0.8352	0.8027	0.5871	0.4324	0.1493	0.0864	0.0011
60	60-57-1	0.3142	0.3142	0.3135	0.3071	0.2819	0.2562	0.1532	0.1054	0.0339	0.0194	0.0012
61	62924-70-3	0.3046	0.3045	0.3038	0.2971	0.2707	0.2442	0.1422	0.0968	0.0307	0.0175	0.00024
62	633-96-5	0.7686	0.7686	0.7686	0.7686	0.7686	0.7686	0.7684	0.7681	0.7457	0.6995	0.0027

ID	CAS	F (0.001 mg)	F (0.01 mg)	F (0.1 mg)	F (1 mg)	F (5 mg)	F (10 mg)	F (50 mg)	F (100 mg)	F (500 mg)	F (1000 mg)	K_e (min ⁻¹)
63	643-79-8	0.9938	0.9938	0.9938	0.9938	0.9938	0.9938	0.9938	0.9938	0.9934	0.9929	0.0014
64	6459-94-5	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.00093
65	6610-29-3	0.4977	0.4977	0.4977	0.4977	0.4977	0.4977	0.4977	0.4977	0.4953	0.4840	0.0024
66	6625-46-3	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0034
67	67-20-9	0.9912	0.9912	0.9912	0.9912	0.9911	0.9910	0.9898	0.9875	0.9150	0.6701	0.0016
68	67747-09-5	0.9904	0.9904	0.9903	0.9902	0.9896	0.9888	0.9742	0.9245	0.4481	0.2716	0.0013
69	68-26-8	0.9807	0.9807	0.9806	0.9799	0.9762	0.9706	0.8870	0.7427	0.2928	0.1729	0.0011
70	68694-11-1	0.9918	0.9918	0.9918	0.9918	0.9917	0.9916	0.9899	0.9856	0.7227	0.4689	0.00044
71	79241-46-6	0.9150	0.9150	0.9145	0.9103	0.8906	0.8646	0.6624	0.4965	0.1742	0.1010	0.0011
72	84-61-7	0.9670	0.9670	0.9668	0.9648	0.9553	0.9415	0.7935	0.6247	0.2304	0.1347	0.0029
73	85509-19-9	0.9813	0.9813	0.9812	0.9805	0.9771	0.9718	0.8933	0.7539	0.3011	0.1782	0.00051
74	86-50-0	0.9902	0.9902	0.9902	0.9899	0.9883	0.9860	0.9459	0.8454	0.3659	0.2190	0.002
75	872-50-4	0.9959	0.9959	0.9959	0.9959	0.9959	0.9959	0.9959	0.9959	0.9959	0.9959	0.0022
76	87392-12-9	0.9951	0.9951	0.9951	0.9951	0.9951	0.9951	0.9948	0.9944	0.9835	0.8928	0.0019
77	87674-68-8	0.9960	0.9960	0.9960	0.9960	0.9960	0.9960	0.9959	0.9959	0.9952	0.9936	0.0021
78	88-58-4	0.9925	0.9925	0.9925	0.9924	0.9924	0.9923	0.9916	0.9901	0.8756	0.6122	0.0012
79	88671-89-0	0.9916	0.9916	0.9916	0.9914	0.9905	0.9892	0.9648	0.8909	0.4072	0.2453	0.0019
80	88-72-2	0.9955	0.9955	0.9955	0.9955	0.9955	0.9955	0.9954	0.9952	0.9906	0.9465	0.0019
81	88-85-7	0.9950	0.9950	0.9950	0.9950	0.9950	0.9950	0.9950	0.9950	0.9950	0.9950	0.002
82	941-69-5	0.9955	0.9955	0.9955	0.9955	0.9955	0.9955	0.9955	0.9954	0.9950	0.9943	0.0019
83	94361-06-5	0.9921	0.9921	0.9921	0.9921	0.9920	0.9918	0.9901	0.9861	0.7296	0.4747	0.0019

ID	CAS	F (0.001 mg)	F (0.01 mg)	F (0.1 mg)	F (1 mg)	F (5 mg)	F (10 mg)	F (50 mg)	F (100 mg)	F (500 mg)	F (1000 mg)	K_e (min ⁻¹)
84	97-77-8	0.8355	0.8354	0.8347	0.8281	0.7985	0.7624	0.5412	0.3939	0.1343	0.0775	0.0024
85	98-51-1	0.9778	0.9778	0.9777	0.9768	0.9724	0.9661	0.8818	0.7463	0.3045	0.1811	0.0024
86	989-38-8	0.9518	0.9518	0.9515	0.9488	0.9359	0.9175	0.7391	0.5641	0.2002	0.1162	0.00041

Figure S2: Bioavailabilities as predicted by the ACD/Labs software for each of 86 EDC.

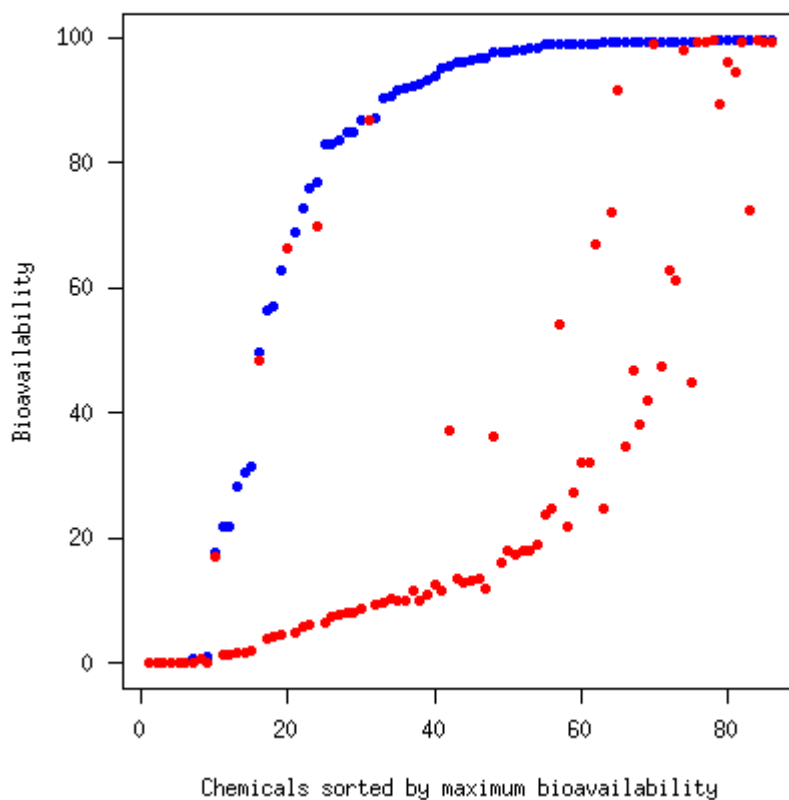


Figure S2: Bioavailability as predicted by ACD/Labs for each of 86 chemicals. The blue and red dots show respectively the bioavailability for oral administration of 0.001 mg and 1000 mg of each chemical.

Figure S3: Histogram of the half-life of each of the 86 EDC.

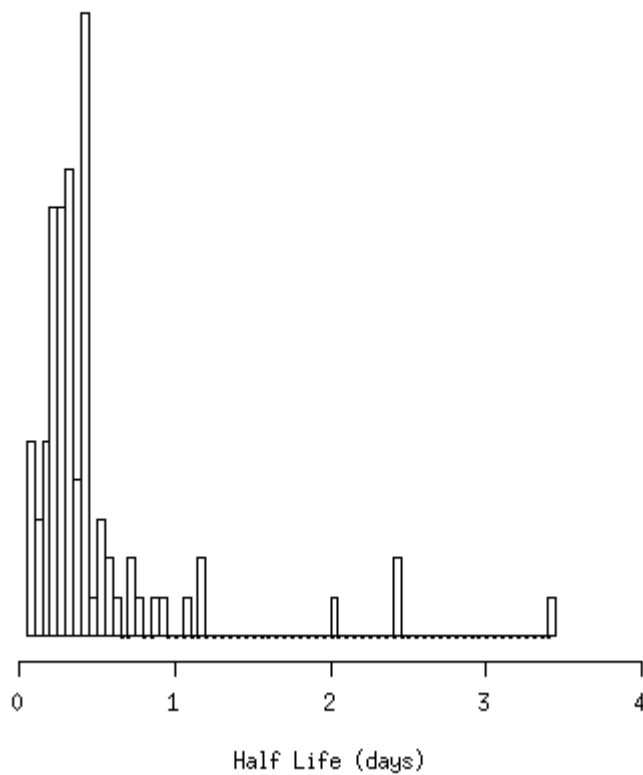


Figure S3: Histogram of the half life of each of the 86 chemicals, calculated from the total body clearance rate constant predicted by ACD/Labs.

Figure S4: Internal concentration vs. exposure rate for of each of the 86 EDC studied.

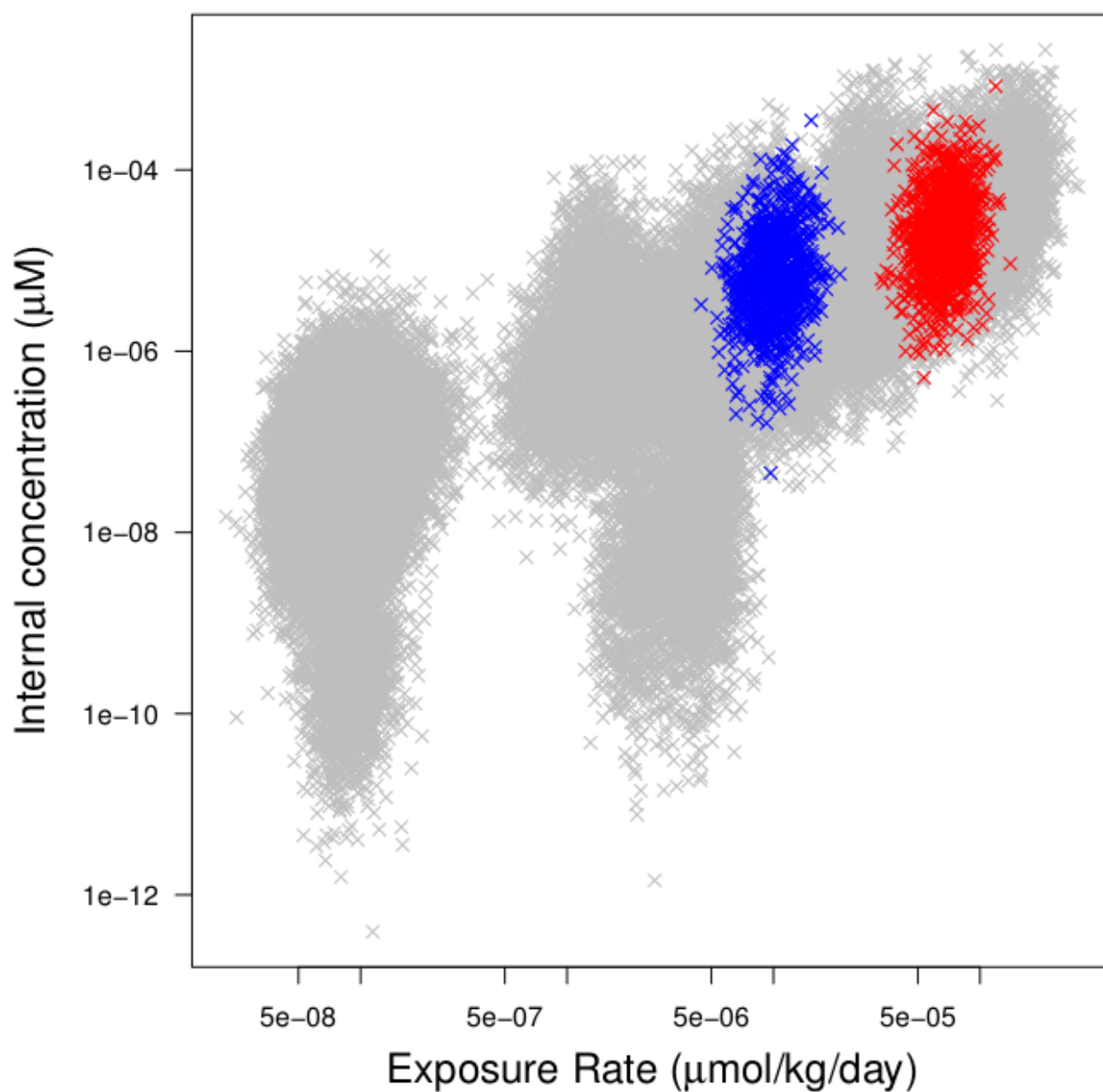


Figure S4: Steady-state internal concentrations of the 86 chemicals studied as a function of exposure levels. Exposures and pharmacokinetic parameters were randomly sampled 10000 times for each chemical (see text), resulting in visible spread. Results for two of the chemicals are highlighted (anastrozole in blue and 4,4'-oxydianiline in red).

Figure S5: Example of a random internal exposure profile.

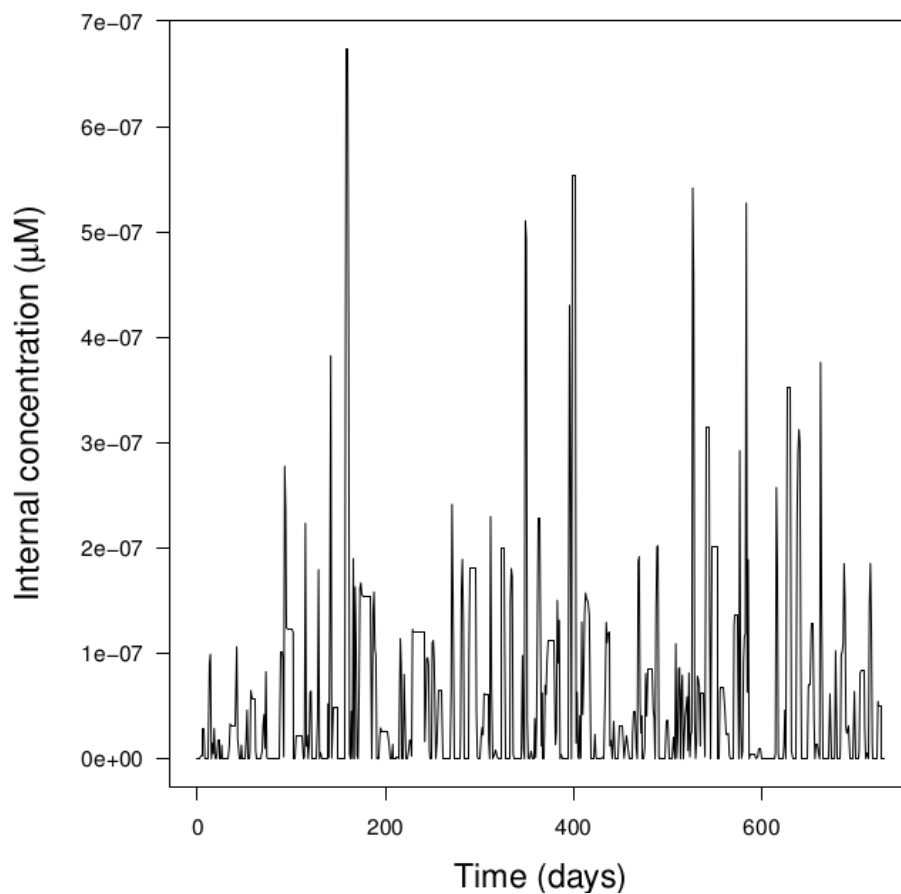


Figure S5: Example of a random internal exposure profile (for lindane). Exposure times and rates were Monte Carlo sampled. Internal exposure as a function of time was obtained by numerical integration of the one-compartment PK model.

Figure S2: Menstrual cycle model equations.

The equations of the menstrual cycle are adapted from Chen and Ward (2013), as indicated.

The differential equation for the dominant follicle mass (F) is a function of a background growth rate, a growth rate component stimulated by FSH according to Hill's model, and a degradation rate under LH control, also according to Hill's model:

$$\frac{\partial F}{\partial t} = \gamma_F + \frac{\beta_F \cdot F \cdot FSH^{m_6}}{EC_{FSH,F}^{m_6} + FSH^{m_6}} - \frac{\gamma_{F,R} \cdot F^2 \cdot LH^{m_7}}{EC_{LH,F}^{m_7} + LH^{m_7}} \quad (1)$$

The ruptured follicle or scar mass (R) is formed from F degradation, with first and converted to *corpus luteum* (C):

$$\frac{\partial R}{\partial t} = \frac{\gamma_{F,R} \cdot F^2 \cdot LH^{m_7}}{EC_{LH,F}^{m_7} + LH^{m_7}} - \gamma_{R,C} \cdot R \quad (2)$$

The differential equation for *corpus luteum* mass is a function of its formation rate from R , and first order degradation:

$$\frac{\partial C}{\partial t} = \gamma_{R,C} \cdot R - \delta_C \cdot C \quad (3)$$

The initial quantities of estradiol ($E2$, in nanograms) and progesterone ($P4$, in nanomoles) in blood and ovaries are given by:

$$Q_{E2,b}(t = 0) = 60 \cdot V_{blood} \quad (4)$$

$$Q_{P4,b}(t = 0) = 10 \cdot V_{blood} \quad (5)$$

$$Q_{E2,o}(t = 0) = 4000 \cdot V_{ovary} \quad (6)$$

$$Q_{P4,o}(t = 0) = 1200 \cdot V_{ovary} \quad (7)$$

The concentration of $E2$ (nanograms/L) and $P4$ (nanomoles/L) in blood and ovaries are:

$$C_{E2,b} = Q_{E2,b} / V_{blood} \quad (8)$$

$$C_{E2,o} = Q_{E2,o} / V_{ovary} \quad (9)$$

$$C_{P4,b} = Q_{P4,b} / V_{blood} \quad (10)$$

$$C_{P4,o} = Q_{P4,o} / V_{ovary} \quad (11)$$

$GnRH$ (arbitrary units) is promoted by blood $E2$, and inhibited by blood $P4$, according to Hill's models:

$$Gn = \frac{E2_b^{m_1}}{EC_{E2,Gn}^{m_1} + E2_b^{m_1}} \cdot \frac{EC_{P4,Gn}^{m_2}}{EC_{P4,Gn}^{m_2} + P4_b^{m_2}} \quad (12)$$

The blood FSH concentration (in $\mu g/L$) in under positive control by past values of $GnRH$ (τ_{FSH} days before) and negative control by current $E2$, according to Hill's models:

$$FSH = \left(FSH_{min} + \frac{(FSH_{max} - FSH_{min}) \cdot Gn_{(t-\tau_{FSH})}^{m_3}}{EC_{Gn_{FSH}}^{m_3} + Gn_{(t-\tau_{FSH})}^{m_3}} \right) \cdot \frac{EC_{E2_{FSH}}^{m_4}}{EC_{E2_{FSH}}^{m_4} + E2_b^{m_4}} \quad (13)$$

The blood LH concentration (in $\mu g/L$) in under positive control by past values of $GnRH$ (τ_{LH} days before), according to Hill's model:

$$LH = LH_{min} + \frac{(LH_{max} - LH_{min}) \cdot Gn_{(t-\tau_{LH})}^{m_5}}{EC_{Gn_{LH}}^{m_5} + Gn_{(t-\tau_{LH})}^{m_5}} \quad (14)$$

The differential equation for $E2$ quantity in blood is a function of transport to and from the ovaries, extra-ovarian production, and elimination rates:

$$\frac{\partial Q_{E2,b}}{\partial t} = F_{ovary}(C_{E2,o} - C_{E2,b}) + Kp_{E2} \cdot \beta_{E2} - Ke_{E2} \cdot C_{E2,b} \quad (15)$$

The differential equation for $E2$ quantity in the ovaries is as a function of its transport to and from blood, and its follicular and luteal production, which can be both affected by endocrine disruption (ED):

$$\frac{\partial Q_{E2,o}}{\partial t} = ED_{cyp19} \cdot Kp_{E2} \cdot (\beta_{E2F} \cdot F + \beta_{E2C} \cdot C) - F_{ovary}(C_{E2,o} - C_{E2,b}) \quad (16)$$

The differential equation for the quantity of $P4$ in blood is a function of its transport to and from the ovaries, extra-ovarian production, and elimination rates:

$$\frac{\partial Q_{P4,b}}{\partial t} = F_{ovary}(C_{P4,o} - C_{P4,b}) + Kp_{P4} \cdot \beta_{P4} - Ke_{P4} \cdot C_{P4,b} \quad (17)$$

The differential equation for the quantity of $P4$ in the ovaries is a function of transport to and from blood, and luteal production:

$$\frac{\partial Q_{P4,o}}{\partial t} = Kp_{P4} \cdot \beta_{P4C} \cdot C - F_{ovary}(C_{P4,o} - C_{P4,b}) \quad (19)$$

Table S3. Menstrual cycle parameter values. Value are from Chen and Ward (2013), except were indicated.

Parameter	Symbol	Value (units)
Ratio of disrupted over control <i>E2</i> synthesis	ED_{CYP19}	- ^a
Time delay for <i>GnRH</i> control of <i>FSH</i>	τ_{FSH}	1 (day)
Time delay for <i>GnRH</i> control of <i>LH</i>	τ_{LH}	1.4 (day)
Baseline <i>E2</i> concentration	β_{E2}	0.1 (ng/L)
Follicular contribution to <i>E2</i> synthesis	$\beta_{E2,F}$	0.48 (ng/L/mass of <i>F</i>)
Luteal contribution to <i>E2</i> synthesis	$\beta_{E2,C}$	0.36 (ng/L/mass of <i>F</i>)
<i>E2</i> clearance from blood	$K_{e,E2}$	1600 (L/day)
<i>E2</i> synthesis scale factor	$K_{p,E2}$	1600 (L/day)
Baseline <i>P4</i> concentration	β_{P4}	0 (nmol/L)
Luteal contribution to <i>P4</i> synthesis	$B_{P4,C}$	0.12 (nmol/L/mass of <i>C</i>)
<i>P4</i> clearance from blood	$K_{e,P4}$	3621 (L/day) ^b
<i>P4</i> synthesis scale factor	$K_{p,P4}$	3621 (L/day)
<i>E2</i> EC_{50} for <i>GnRH</i> secretion promotion	$EC_{E2,Gn}$	185 (ng/L)
<i>E2</i> Hill exponent for <i>GnRH</i> secretion	m_1	2 (unitless)
<i>P4</i> EC_{50} for <i>GnRH</i> secretion inhibition	$EC_{P4,Gn}$	10 (nmol/L)
<i>P4</i> Hill exponent for <i>GnRH</i> secretion inhibition	m_2	2 (unitless)
<i>GnRH</i> EC_{50} for <i>FSH</i> secretion promotion	$EC_{Gn,FSH}$	0.453 (arbitrary units)
<i>GnRH</i> Hill exponent for <i>FSH</i> secretion promotion	m_3	2 (unitless)
<i>E2</i> EC_{50} for <i>FSH</i> secretion inhibition	$EC_{E2,FSH}$	432 (ng/L)
<i>E2</i> Hill exponent for <i>FSH</i> secretion inhibition	m_4	4 (unitless)
Minimum <i>FSH</i> concentration	FSH_{min}	28.5 (μg/L)
Maximum <i>FSH</i> concentration	FSH_{max}	500 (μg/L)
<i>GnRH</i> EC_{50} for <i>LH</i> release	$EC_{Gn,LH}$	0.447 (arbitrary units)
<i>GnRH</i> Hill exponent for <i>LH</i> release	m_5	10 (unitless)
Minimum <i>LH</i> concentration	LH_{min}	36.4 (μg/L)

Maximum <i>LH</i> concentration	LH_{max}	676 (µg/L)
Baseline follicle growth rate	γ_F	0 (arbitrary units/day)
<i>FSH</i> EC_{50} for follicle growth stimulation	$EC_{FSH,F}$	150 (µg/L)
<i>FSH</i> Hill exponent for follicle growth stimulation	m_6	2 (unitless)
<i>FSH</i> enhanced follicle growth stimulation rate constant	β_F	2.1 (1/day)
<i>LH</i> EC_{50} for follicle rupture	$EC_{LH,F}$	325 (µg/L)
<i>LH</i> Hill exponent for follicle rupture	m_7	2 (unitless)
Follicle rupture rate constant per unit follicle mass	$\gamma_{F,R}$	0.06 (1/day/arbitrary units)
<i>R</i> to <i>C</i> conversion rate constant	$\gamma_{R,C}$	0.285 (1/day)
<i>Corpus luteum</i> decay rate constant	δ_C	0.345 (1/day)
Blood volume	V_{blood}	4.1 (L) ^c
Ovaries volume	V_{ovary}	0.2 (L) ^c
Ovaries blood flow	F_{ovary}	30 (L/day) ^c

^a The value of this parameter depends on exposure to endocrine disrupting chemicals.

^b Little et al. (1966).

^c International Commission on Radiological Protection (ICRP) (2002).

Table 4: Menstrual cycle initial state variables' values.

State variable	Symbol	Value (units)
Dominant follicle mass	F	79.48 (arbitrary units)
Ruptured follicle (scar) mass	R	20.23 (arbitrary units)
<i>Corpus luteum</i> mass	C	33.35 (arbitrary units)
Quantity of estradiol in blood	$Q_{E2,b}$	206.1 (ng)
Quantity of estradiol in ovaries	$Q_{E2,o}$	545.1 (ng)
Quantity of progesterone in blood	$Q_{P4,b}$	16.43 (nmol)
Quantity of progesterone in ovaries	$Q_{P4,o}$	97.53 (nmol)

Figure S6: Simulation of normal ovarian cycling and comparison to data.

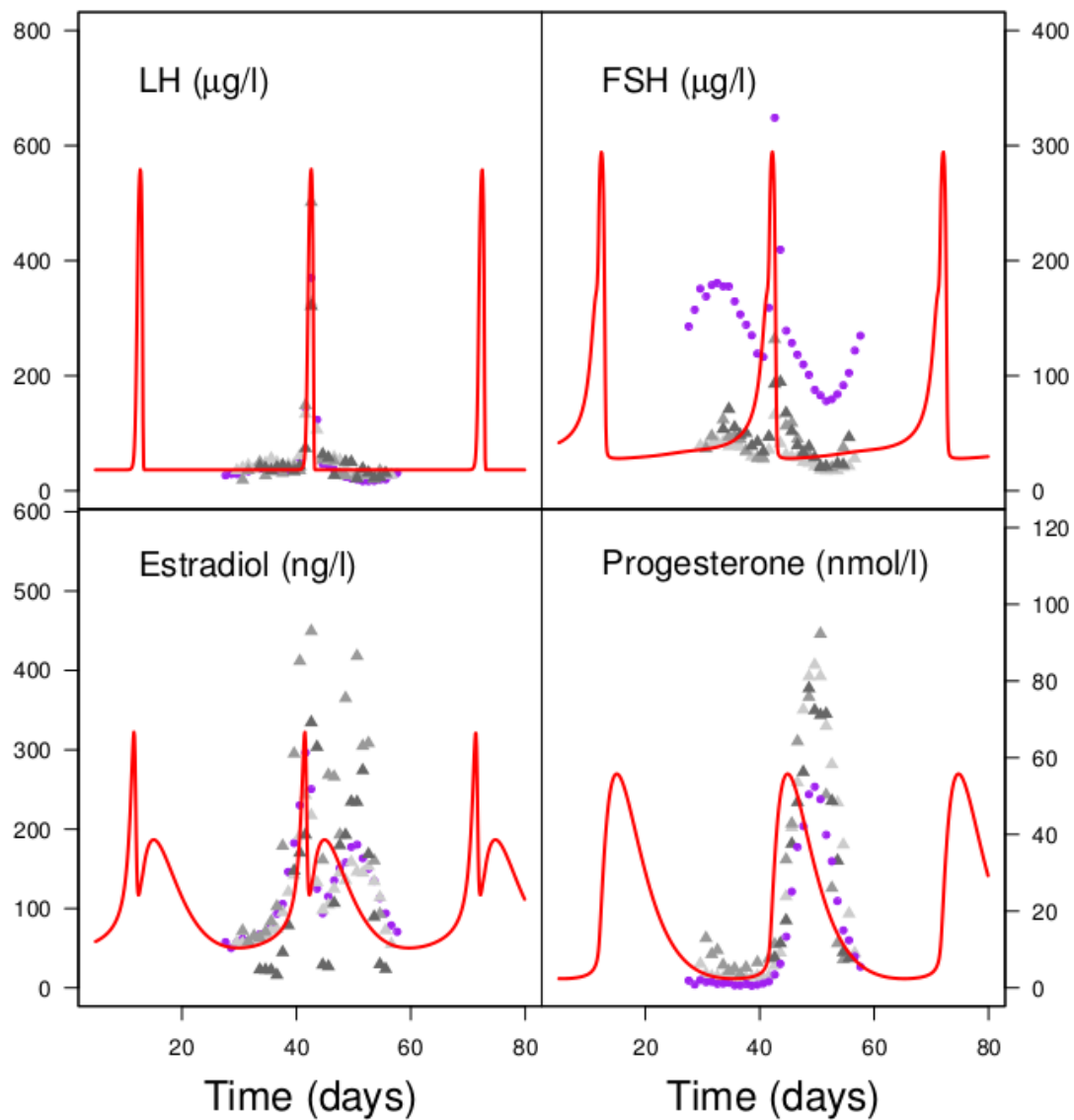


Figure S6: Model simulated time course of *LH*, *FSH*, *E2* and *P4* during normal human ovarian cycles (red lines). The model equations and parameter values used are given in Methods S2 and Tables S3 and S4 above. Data are overlaid as points: purple circles from McLachlan et al. (1990, Fig. 1); gray triangles from Welt et al. (1999). The LH data points from Welt *et al.* were rescaled so that their baseline values match with those of McLachlan et al. The same rescaling factor was applied to Welt et al. FSH data.

Figures S7-S10: Simulation of normal and perturbed ovarian cycling.

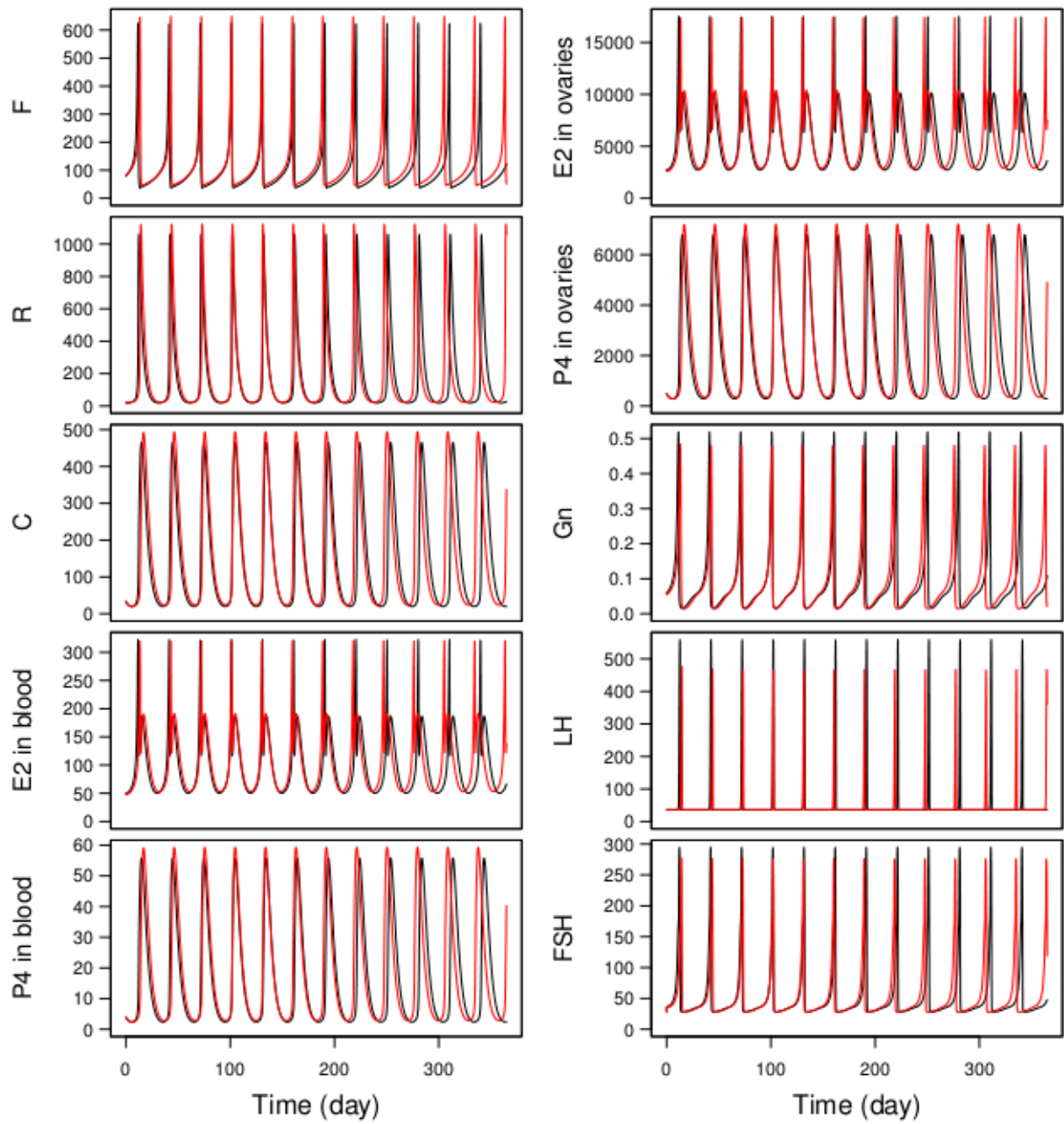


Figure S7: Simulated time course of all model variables during normal ovarian cycles (parameter ED_{CYP19} set to 1, black lines) and with a 5% constant inhibition of aromatase (parameter ED_{CYP19} set to 0.95). The model equations and parameter values used are given in Methods S2 and Tables S3 and S4 above. LH and FSH units are in $\mu\text{g/L}$. $GnRH$ units are arbitrary, the units of the other variables are given in Table S4 above. The perturbed cycle differs only slightly from normal.

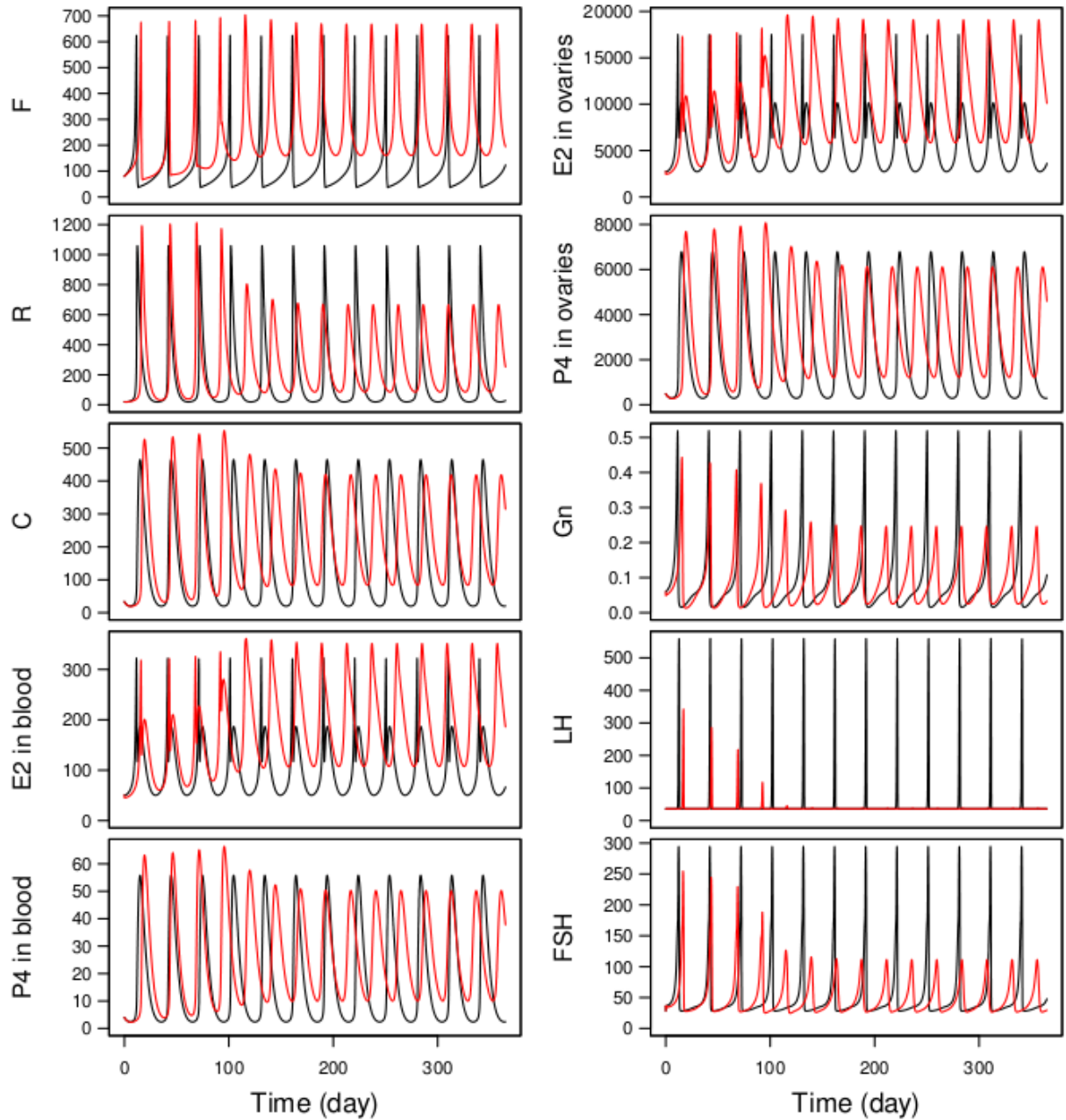


Figure S8: Simulated time course of all model variables during normal ovarian cycles (parameter ED_{CYP19} set to 1, black lines) and with A 10% constant inhibition of aromatase (parameter ED_{CYP19} set to 0.9). The model equations and parameter values used are given in Methods S2 and Tables S3 and S4 above. LH and FSH units are in $\mu\text{g/L}$. $GnRH$ units are arbitrary, the units of the other variables are given in Table S4 above. LH peaks disappear rapidly and the systems bifurcates to a new solution.

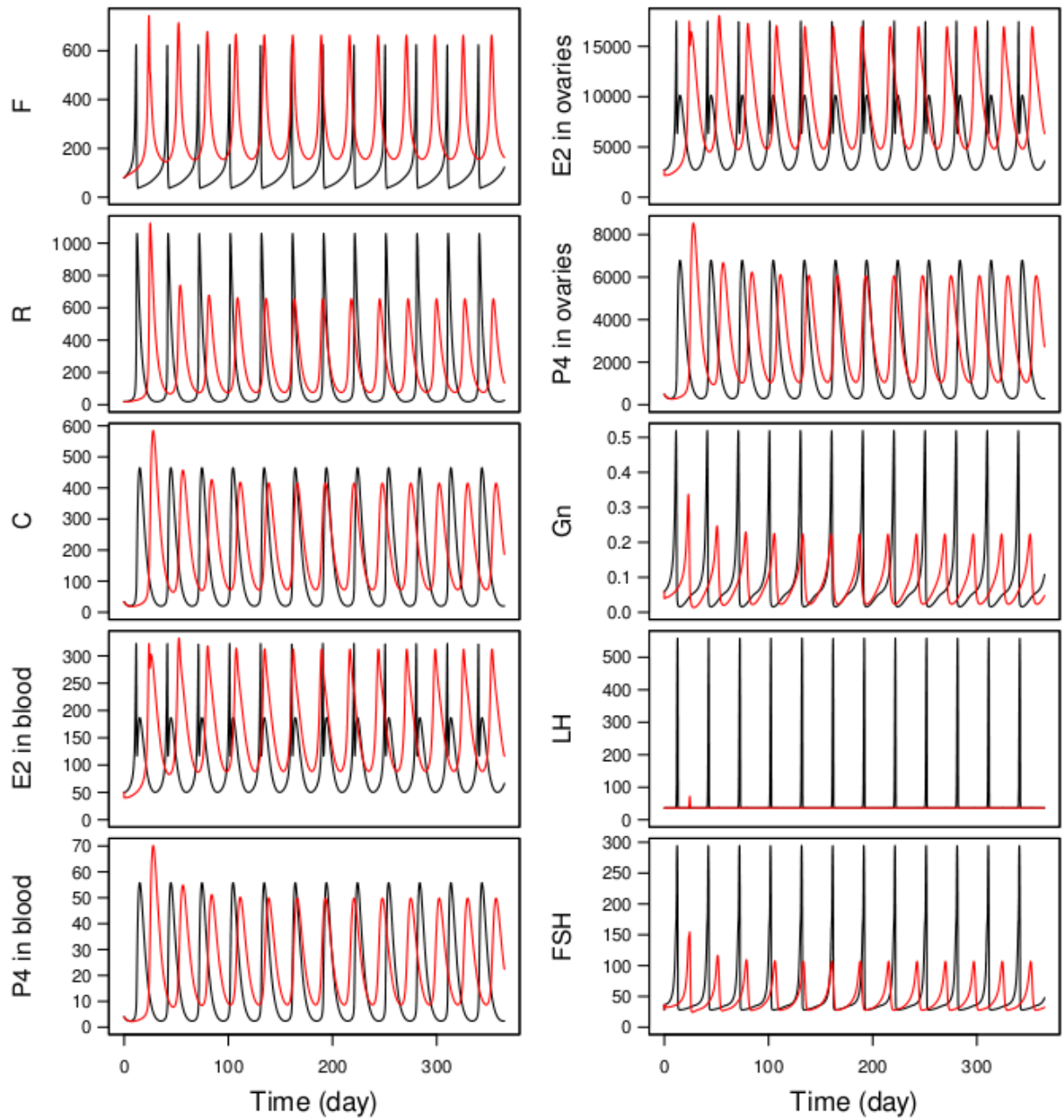


Figure S9: Simulated time course of all model variables during normal ovarian cycles (parameter ED_{CYP19} set to 1, black lines) and with A 20% constant inhibition of aromatase (parameter ED_{CYP19} set to 0.8). The model equations and parameter values used are given in Methods S2 and Tables S3 and S4 above. LH and FSH units are in $\mu\text{g/L}$. $GnRH$ units are arbitrary, the units of the other variables are given in Table S4 above. The cycle is profoundly disrupted.

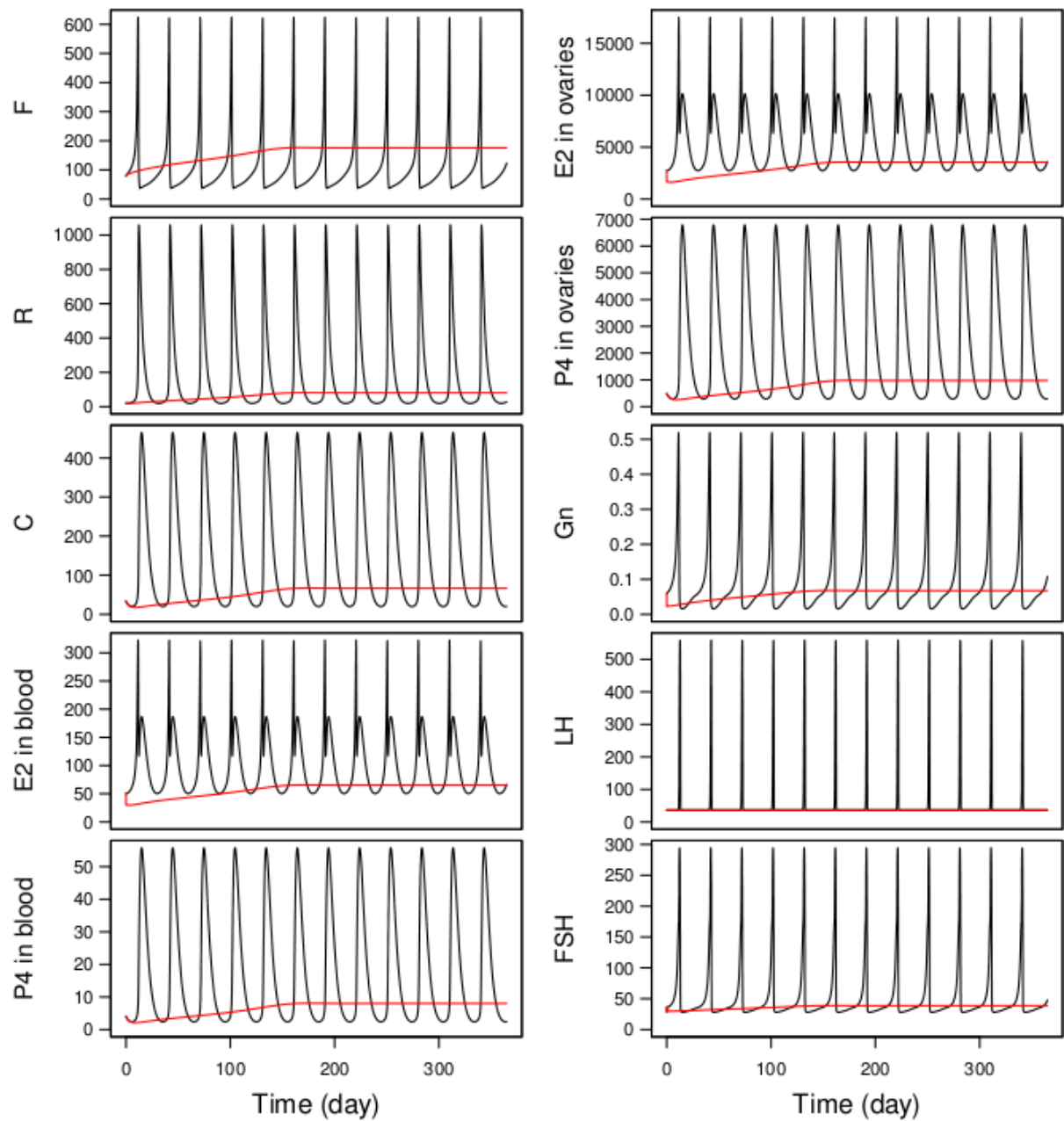


Figure S10: Simulated time course of all model variables during normal ovarian cycles (parameter ED_{CYP19} set to 1, black lines) and with A 40% constant inhibition of aromatase (parameter ED_{CYP19} set to 0.6). The model equations and parameter values used are given in Methods S2 and Tables S3 and S4 above. LH and FSH units are in $\mu\text{g/L}$. $GnRH$ units are arbitrary, the units of the other variables are given in Table S4 above. The cycle is totally disrupted.

Figure S11: Simulation of estradiol time profiles during time-varying exposures to 86 EDCs.

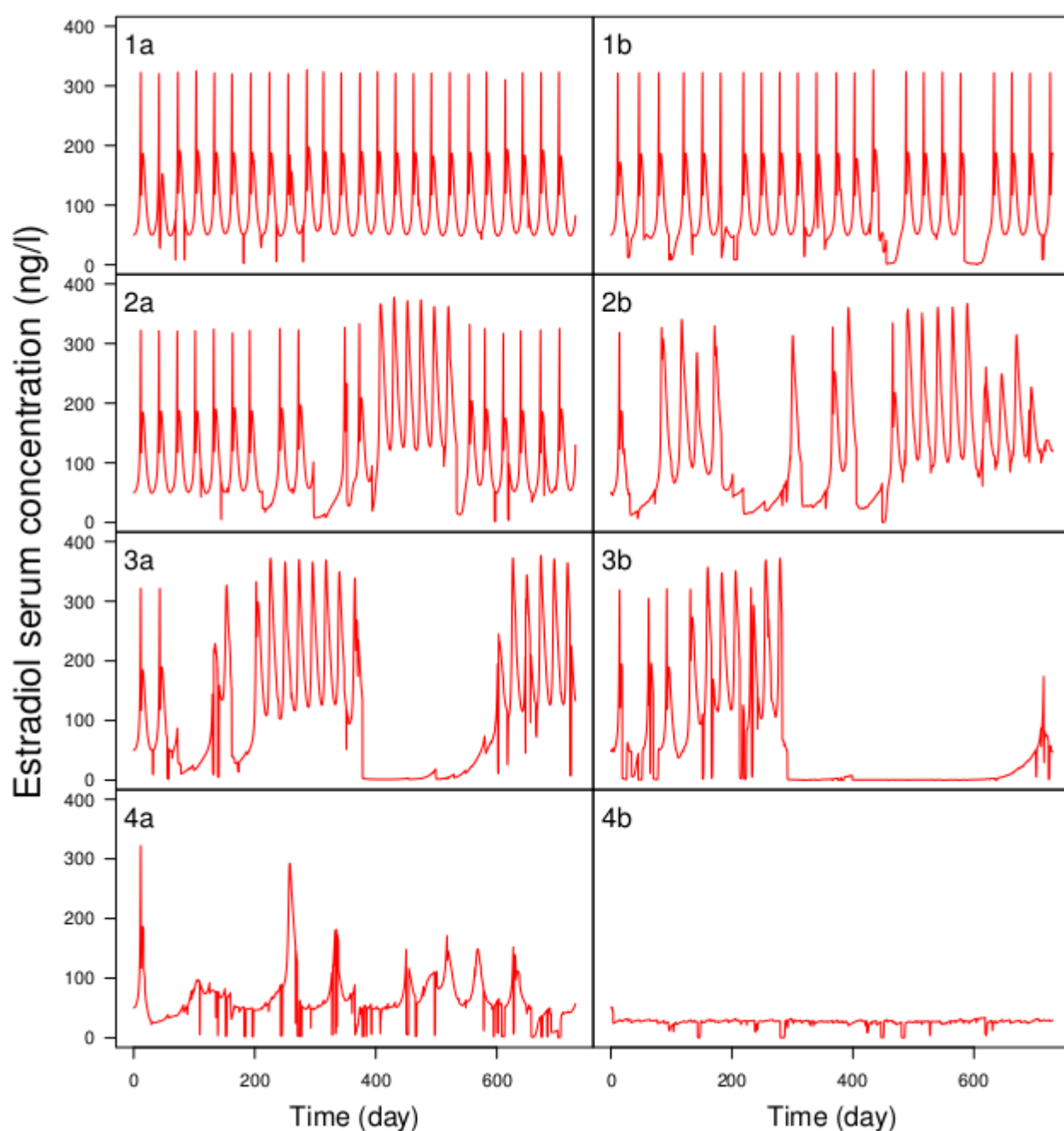


Figure S11: Typical simulated time profiles of estradiol concentration during time-varying exposures to random mixtures of 86 aromatase inhibitors. Four classes (rows) of increasing disruption are illustrated (see main text). Left column: least disrupted profile in its class; Right column: most disrupted. Panel 1a shows a practically normal profile with regular ovulation peaks. Panel 4b shows complete disruption.

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